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# Enhancement of isothermal entropy change due to spin fluctuations in itinerant-electron metamagnetic La(Fe<sub>0.88</sub>Si<sub>0.12</sub>)<sub>13</sub> compound

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# Abstract

A large isothermal entropy change in La(Fe<sub>0.88</sub>Si<sub>0.12</sub>)<sub>13</sub> itinerant-electron metamagnetic (IEM) compound has been investigated by using the Maxwell and Clausius–Clapeyron relations. The entropy change obtained from the Clausius–Clapeyron relation  $\Delta S_m^{CC}$  gradually decreases with increasing temperature, while that from the Maxwell relation  $\Delta S_m^{Mx}$  in the magnetic field of 2 T shows a plateau-like behavior in 195–203 K. The difference between  $\Delta S_m^{Mx}$  and  $\Delta S_m^{CC}$  is mainly explained by the entropy change in the paramagnetic (P) state below the critical magnetic field of the IEM transition  $B_C$ . In the P state, the temperature dependence of susceptibility  $\chi_p$  is enhanced by spin fluctuations. The thermal variation of  $|\Delta S_m^{Mx} - \Delta S_m^{CC}|$  is well represented by taking that of  $\chi_p$  as well as  $B_C$  into account. Therefore, the plateau-like behavior of  $\Delta S_m^{Mx}$  comes from the enhancement of the entropy change in the P state, which cancels the decrease of  $\Delta S_m^{CC}$  due to the decrease of latent heat of the IEM transition with increasing temperature.

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### 1. Introduction

Recently, we have demonstrated that  $La(Fe_xSi_{1-x})_{13}$  compounds exhibit the thermal-induced first-order ferromagnetic (F)-paramagnetic (P) phase transition at the Curie temperature  $T_{\rm C}$ , as well as the itinerant-electron metamagnetic (IEM) transition, that is, a magnetic-field induced P-F phase transition just above  $T_{\rm C}$  [1–4]. The IEM transition exhibits large magnetocaloric effects (MCEs) such as large values of the isothermal entropy change  $\Delta S_{\rm m}$  and the adiabatic temperature change  $\Delta T_{ad}$  [5–10]. The large MCEs of the above compounds attract much attention in the field of both the fundamental research of thermodynamic characteristics of the IEM transition and the practical application of highperformance magnetic refrigerants. For the latter field, the value of  $T_{\rm C}$  has been elevated up to room temperature by hydrogen absorption in La(Fe<sub>x</sub>Si<sub>1-x</sub>)<sub>13</sub>H<sub>y</sub> [11,12] and the large MCEs are obtained in the range of 180-330 K, depending on the hydrogen concentration y [7,8,13].

It has been pointed out that the entropy change  $\Delta S_m$  in La(Fe<sub>x</sub>Si<sub>1-x</sub>)<sub>13</sub> compounds is enhanced by the large latent heat of the IEM transition related to a large magnetization change [7–9]. Furthermore, the IEM transition at finite temperature is closely correlated with the thermal variation of spin fluctuations [14,15]. In itinerant-electron systems, spin fluctuations act as dominant elementally excitations, renormalizing the magnetic free energy[16]. In other words, the thermal variation of spin fluctuations governs the magnetic entropy, especially in the P state. Accordingly, the isothermal magnetic entropy change  $\Delta S_m$  is also related to spin fluctuations.

In the present study, the thermal variation of  $\Delta S_{\rm m}$  related to the IEM transition in La(Fe<sub>0.88</sub>Si<sub>0.12</sub>)<sub>13</sub> compound is investigated by using the Maxwell and the Clausius–Clapeyron relations. The obtained results are discussed in terms of the contribution of spin fluctuations to  $\Delta S_{\rm m}$ .

## 2. Experimental

 $La(Fe_{0.88}Si_{0.12})_{13}$  compound was prepared by arc-melting in an argon gas atmosphere. To obtain NaZn<sub>13</sub>-type single

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phase, the specimen was annealed in a vacuum quartz tube at 1323 K for 10 days. The magnetization was measured with a superconducting quantum interference device (SQUID) magnetometer. The specific heat measurements were carried out by a relaxation method.

# 3. Results and discussion

Fig. 1 shows the temperature dependence of the entropy change obtained from the Clausius–Clapeyron relation,  $\Delta S_m^{CC}$  together with the absolute value of  $|\Delta S_m^{Mx}|$  from the Maxwell relation in the magnetic field change from 0 T to  $B_{max} = 2$  T for La(Fe<sub>0.88</sub>Si<sub>0.12</sub>)<sub>13</sub>. From the thermodynamic relation, the Clausius–Clapeyron relation gives the entropy change  $\Delta S_m^{CC}$  due to the latent heat of the first-order magnetic phase transition as follows:

$$\Delta S_{\rm m}^{\rm CC} = \Delta M \frac{{\rm d}B_{\rm C}}{{\rm d}T},\tag{1}$$

where  $B_{\rm C}$  and  $\Delta M$  are the thermodynamic IEM transition field and the change in magnetization at  $B_{\rm C}$ . As shown in Fig. 1,  $\Delta S_{\rm m}^{\rm CC}$  is consistent with the entropy change q/T due to the latent heat q obtained from the specific measurements. Eq. (1) is derived from the condition that the Gibbs energy at  $B = B_{\rm C}$  in the F and the P states equals in magnitude. Therefore,  $\Delta S_{\rm m}^{\rm CC}$  is scarcely influenced by the magnetic entropy change in the P state in  $B < B_{\rm C}$  and that in the F state in  $B > B_{\rm C}$ . On the other hand, the following equation associated with the Maxwell relation gives the magnetic entropy change in the magnetic field change from 0 to  $B_{\rm max}$ :

$$\Delta S_{\rm m}^{\rm Mx} = \int_0^{B_{\rm max}} \frac{{\rm d}M}{{\rm d}T} {\rm d}B. \tag{2}$$

Therefore, the entropy changes in the P and F states below and above  $B_{\rm C}$  are also involved. Although the behavior of  $\Delta S_{\rm m}^{\rm Mx}$  changes with  $B_{\rm max}$ , the discussion is dedicated on the data in  $B_{\rm max} = 2$  T, because the thermal induced transition above



Fig. 1. Temperature dependence of the magnetic entropy change for La(Fe<sub>0.88</sub>Si<sub>0.12</sub>)<sub>13</sub> obtained from the Clausius–Clapeyron relation  $\Delta S_m^{CC}$ , absolute value of that from the Maxwell relation  $\left|\Delta S_m^{Mx}\right|$  in the magnetic field change from 0 to 2 T, together with the values of latent heat divided by temperature, q/T, obtained from the specific heat data.

2 T becomes relatively broad [7,8], interrupting the precise evaluation of latent heat. Furthermore, from practical view point of magnetic cooling,  $B_{\text{max}} = 2 \text{ T}$  is approximately the highest value of flux density of high-performance permanent magnets desired to be used in magnetic refrigerators.

It has been revealed that the temperature dependence of  $B_{\rm C}$  is almost proportional to T [7], and hence  $dB_{\rm C}/dT$  of about 0.22 T/K is hardly changed in a temperature range of 195–203 K. On the other hand,  $\Delta M$  at  $B_{\rm C}$  decreases in a manner as  $(\Delta M)^2 \propto T$  [9]. Therefore, the value of  $\Delta S_{\rm m}^{\rm CC}$ decreases from 19 J/(kg K) at 195 K to 9 J/(kg K) at 203 K. On the contrary, the temperature dependence of  $\left|\Delta S_{m}^{Mx}\right|$  shows a plateau-like behavior around 20-18 J/(kg K) in the temperature range between 195 and 203 K. The difference between  $\Delta S_{\mathrm{m}}^{\mathrm{CC}}$  and  $\left|\Delta S_{\mathrm{m}}^{\mathrm{Mx}}\right|$  becomes larger with increasing temperature, and  $\Delta S_{\rm m}^{\rm CC}$  becomes about a half of  $\left|\Delta S_{\rm m}^{\rm Mx}\right|$  at 203 K. It is well-known that the first-order phase transition is accompanied by nucleation and growth processes. In increasing magnetic field, the nucleation of the F region does not start just at  $B_{\rm C}$ , but at  $B_1$  which is higher than  $B_{\rm C}$  due to the energy barrier. Furthermore, the IEM transition proceeds within a certain width of magnetic field  $\delta_{\rm B}$  above the onset field of the transition  $B_1$  because of growth process of the nucleated F regions in the P matrix. Therefore, Eq. (2) is rewritten as the sum of three terms as follows [17,18]:

$$\Delta S_{\rm m} = \Delta S^{\rm P} + \Delta S^{\rm Tr} + \Delta S^{\rm F} \tag{3}$$

with

$$\Delta S^{\mathrm{P}} = \int_{0}^{B_{1}} \frac{\partial M}{\partial T} \mathrm{d}B, \qquad \Delta S^{\mathrm{Tr}} = \int_{B_{1}}^{B_{2}} \frac{\partial M}{\partial T} \mathrm{d}B \qquad \text{and}$$
$$\Delta S^{\mathrm{F}} = \int_{B_{2}}^{B_{\mathrm{max}}} \frac{\partial M}{\partial T} \mathrm{d}B$$

where  $B_2$  is defined as  $B_1 + \delta_B$ . The term  $\Delta S^{\text{Tr}}$  in Eq. (3) is related to the IEM transition and should be close to  $\Delta S_m^{\text{CC}}$  when  $\delta_B$  is small because of differentiability of *T* and *B* for the Gibbs energy. Consequently, the difference between  $|\Delta S_m^{\text{MX}}|$  and  $\Delta S_m^{\text{CC}}$  is attributed to the rest of terms in Eq. (3) apart from  $\Delta S^{\text{Tr}}$ , i.e., the  $\Delta S^{\text{P}}$  and  $\Delta S^{\text{F}}$  denoting the entropy change in the P and F states by applying magnetic field, respectively.

In order to elucidate the relation between  $|\Delta S_m^{Mx}|$  and  $\Delta S_m^{CC}$  described above, the values of  $\Delta S_m^{Mx}$  at T = 198 and 200 K are plotted against  $B_{max}$  in Fig. 2. In order to evaluate the values of  $B_1$  and  $B_2$ , the fitting of magnetization curves are made in the inset by taking into account the following relation derived from the Landau expansion theory [14].

$$B = a(T)M + b(T)M^{3} + c(T)M^{5}$$
(4)

with

$$a(T) = a(0) + \frac{5}{3}b(0)\xi(T)^2 + \frac{35}{9}c(0)\xi(T)^4,$$
  
$$b(T) = b(0) + \frac{14}{3}c(0)\xi(T)^2, \qquad c(T) = c(0)$$



Fig. 2. Magnetic entropy change for  $La(Fe_{0.88}Si_{0.12})_{13}$  at 198 and 200 K plotted against the maximum value of magnetic field change  $B_{max}$ . The notations  $B_1$  and  $B_2$  are explained in the text. The inset shows the magnetization curve at 198 K. The dotted curve represents the fitting result. Two vertical dashed lines stand for the thermodynamic ( $B_C$ ) and the onset critical ( $B_1$ ) fields for the IEM transition.

where  $\xi(T)^2$  is the mean square amplitude of spin fluctuations. The IEM transition appears above  $T_{\rm C}$  under the condition of a(0) > 0, b(0) < 0, c(0) > 0 with 3/16 > a(0)b(0)/c(0) > 5/28. Shown in the inset in Fig. 2 is the magnetization curve at 198 K, together with the fitting result. The value of  $B_1$  is determined from the fitting as the boundary where Eq. (4) changes from the multivalue function to the single-value one. On the other hand, Eq. (4) is given without the nucleation and growth processes, therefore, the value of  $B_2$  is defined experimentally as a closing point of hysteresis above  $B_1$ . The  $\Delta S_{\rm m}^{\rm Mx} - B_{\rm max}$  curves are nonlinear in analogy with the magnetization curves, and the steepest change is observed between  $B_1$  and  $B_2$ . With increasing temperature, the region between 0 to  $B_1$  becomes wider, whereas that between  $B_2$  and  $B_{\text{max}}$ (=2T) becomes narrower due to the increase of  $B_{\rm C}$  against temperature. It should be noticed that  $B_2$  is larger than 2 T at temperatures above 201 K, therefore,  $\Delta S^{\text{F}}$  in Eq. (3) has no influence on  $\Delta S_{\rm m}^{\rm Mx}$  and the integration region of  $\Delta S^{\rm Tr}$  given in Eq. (3) is truncated. On the other hand, the value of  $\Delta S_m^{Mx}$ from 0 to  $B_1$  becomes larger with increasing temperature.

Since no spontaneous magnetic moment exists in the P state, the magnetization *M* equals to the product of susceptibility  $\chi_p$  and magnetic field *B*. Consequently,  $\partial M/\partial T$  under the constant magnetic field *B* in Eq. (2) is dominated by  $B(\partial \chi/\partial T)$ . It has been discussed that the paramagnetic susceptibility of itinerant electron systems is influenced by the amplitude of thermal spin fluctuations  $\xi$  due to the renormalization of free energy by spin fluctuations [14–16].

It is well-known that the temperature dependence of  $\chi_p$  exhibits a maximum at  $T_{max}$  in many IEM compounds[15]. Although  $\chi_p$  of La(Fe<sub>x</sub>Si<sub>1-x</sub>)<sub>13</sub> compounds decreases continuously against temperature in ambient pressure[4], the maximum phenomenon is observed in  $\chi_p$  by applying hydrostatic pressure close to the critical value of disappearance in the ferromagnetic ground state [19]. Therefore, it is apparent



Fig. 3. Temperature dependence of the inverse magnetic susceptibility  $1/\chi$  obtained from the thermomagnetization measurement in 0.5 T for La(Fe<sub>0.88</sub>Si<sub>0.12</sub>)<sub>13</sub> compound.

that  $\chi_p$  of the present compound is also dominated by spin fluctuations. To account for the influence of spin fluctuations on  $\chi_p$  in La(Fe<sub>0.88</sub>Si<sub>0.12</sub>)<sub>13</sub>, the temperature dependence of inverse magnetic susceptibility  $1/\chi_p$  obtained from the thermomagnetization measurement in 0.5 T is plotted in Fig. 3. The temperature dependence of  $1/\chi_p$  exhibits a Curie–Weiss like behavior. Therefore, the effective magnetic moment  $p_{eff}$ is obtained from the following relation:

$$\chi_{\rm p} = \frac{C}{(T - \theta_{\rm p})} = \frac{\mu_B^2 p_{\rm eff}^2}{3k_B(T - \theta_{\rm p})}$$
(5)

By the least square fitting,  $p_{eff}$  is evaluated to be 3.9  $\mu_B$ /Featom, being about two times larger than the spontaneous magnetic moment  $p_s = 2.0 \,\mu_B$ /Fe-atom at 4.2 K. Generally, the ratio  $p_{\rm eff}/p_{\rm s}$  becomes almost unity in localized magnetic moment systems because the local amplitude of magnetic moment is independent of temperature [16]. On the other hand, the ratio becomes larger than unity in itinerant electron systems due to thermal variation of amplitude of spin fluctuations [16]. The values of  $p_{\rm eff}/p_{\rm s}$  of itinerant electron ferromagnets are correlated with the Curie temperature. In plots of  $p_{\rm eff}/p_{\rm s}$  against  $T_{\rm C}$ , which is called the Rhodes–Wohlfarth plot; a characteristic increase of  $p_{\rm eff}/p_{\rm s}$  with decreasing  $T_{\rm C}$ towards 0 is common to many kinds of itinerant electron magnets [20,21]. Although the phase transition at  $T_{\rm C}$  of the present compound is of first-order in contrast to conventional ferromagnets exhibiting second-order transitions, the value of  $p_{\rm eff}/p_{\rm s}$  is close to other itinerant-electron magnets with  $T_{\rm C}$ around 200 K.

From Eqs. (3) and (5), the relation between  $\Delta S^{P}$  and the Curie constant *C* is expressed as

$$\Delta S^{\mathrm{P}} = \int_{0}^{B_{1}} \left( \frac{B \partial \chi_{\mathrm{p}}}{\partial T} \right)_{B} \mathrm{d}B = -\frac{C}{2(T-\theta_{\mathrm{p}})^{2}} B_{1}^{2} \tag{6}$$

Therefore, the enhancement of  $p_{\text{eff}}$  and *C* due to spin fluctuations enlarges  $\Delta S^P$ . Furthermore, it is worth noting that the values of  $B_1$  and  $B_C$  show almost the same temperature dependence. As mentioned already, the temperature dependence of  $B_C$  has been reported to be proportional to  $T - T_C$  [7], and hence,  $\Delta S^P$  is proportional to  $Cg^2(T - T_C)^2/(T - \theta_p)^2$ , where *g* is the coefficient in  $B_C = g(T - T_C)$ . In Fig. 4, the tempera-



Fig. 4. Thermal variation of difference between the absolute value of the entropy change obtained from the Maxwell relation and the value from the Clausius–Clapeyron relation,  $\left|\Delta S_m^{Mx}\right| - \Delta S_m^{CC}$ , together with the calculated line from Eq. (6).

ture dependence of  $|\Delta S_{\rm m}^{\rm Mx}| - \Delta S_{\rm m}^{\rm CC}$  obtained from Fig. 1 is compared to the numerical evaluation of Eq. (6) by putting the values of g = 0.22 T/K, C = 246 J K/(kg T<sup>2</sup>),  $T_{\rm C} = 195$  K and  $\theta_{\rm p} = 192$  K. The thermal variation of  $|\Delta S_{\rm m}^{\rm Mx}| - \Delta S_{\rm m}^{\rm CC}$ is represented by the calculated values of Eq. (6), excepting around 196 K where the contribution of  $\Delta S^{\rm F}$  in Eq. (3) makes  $|\Delta S_{\rm m}^{\rm Mx}| - \Delta S_{\rm m}^{\rm CC}$  slightly larger than the calculated one. Furthermore, a slight difference between the experimental and the calculated results around 200–203 K arises from a saturated behavior of  $|\Delta S_{\rm m}^{\rm Mx}| - \Delta S_{\rm m}^{\rm CC}$  due to the truncated contribution of  $\Delta S^{\rm Tr}$  associated with the relation  $B_1 < B_{\rm max} = 2 \text{ T} < B_2$  at these temperatures. Apart from such slight difference, it is clear that the increase of  $\Delta S_{\rm m}^{\rm P}$ with temperature mainly cancels the decrease of the latent heat, resulting in the plateau-like behavior of  $\Delta S_{\rm m}^{\rm Mx}$  around 196–202 K.

#### 4. Conclusion

Influence of spin fluctuations on the isothermal entropy change  $\Delta S_{\rm m}$  has been investigated for La(Fe<sub>0.88</sub>Si<sub>0.12</sub>)<sub>13</sub> itinerant-electron metamagnetic (IEM) compound. The entropy change obtained from the Clausius–Clapeyron relation,  $\Delta S_{\rm m}^{\rm CC}$ , continuously decreases against temperature above  $T_{\rm C}$  = 195 K, while that obtained from the Maxwell relation  $\Delta S_{\rm m}^{\rm Mx}$  obtained in the magnetic field change from 0 to  $B_{\rm max}$  = 2 T exhibits a plateau-like behavior in a temperature range of 196–203 K. Taking the thermal variation of the latent heat and the critical field of the IEM transition into account, the difference between  $\Delta S_m^{CC}$  and  $|\Delta S_m^{Mx}|$  can be explained by the entropy change in the paramagnetic (P) state,  $\Delta S^P$ . From the Maxwell relation, the magnitude of  $\Delta S^P$  below the onset transition field  $B_1$  is related to the thermal variation of paramagnetic susceptibility  $\chi_p$ . The thermal variation of  $\chi_p$ shows a Curie–Weiss like behavior with a large Curie constant *C* due to the thermal variation of spin fluctuations. In consequence, the value of  $\Delta S^P$  is enhanced by spin fluctuations. By considering the thermal variations of  $\chi_p$  and the critical field  $B_C$ , it is concluded that the thermal increase of  $\Delta S^P$  cancels the decrease of the latent heat against temperature, resulting in the plateau-like behavior of  $\Delta S_m^{Mx}$ .

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